

## Tillämpad AI

### Föreläsning 3, spelprogram I

## Why Game-Playing?

- Simple to formulate and describe
- Limited and clear domain
- Does not need lots of general knowledge
- Easy to test
- Supposed to demand intelligence
- Fun...

## Computer Chess

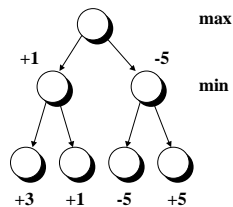
- Branching factor ~36
- Depth > 40 moves (= 80 half moves or plies)
- $N = 36^{80} >$  the number of atoms that would fill the visible universe
- Heuristics needed

## Parts of a Chess Program

- Move generator(s)
- Make/retract - operators to make moves
- Evaluation function
- Search method
- High efficiency

## Minimax Search

- Needs evaluation function
- Depth First
- Fixed depth
- Optimal solution within search horizon
- Efficient to implement



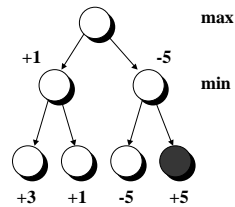
## Minimax

```
int NegMax ()
{
    int v, Max = - MAXVALUE;

    if (Ply == MaxPly) return WhiteToMove ? Eval () : - Eval ();
    GenerateMoves ();
    loop (Move) {
        Make (Move); Ply ++;
        v = - NegMax ();
        Ply --; Retract (Move);
        if (v > Max) Max = v;
    }
    return Max;
}
```

## Alpha-Beta Algorithm

- Equivalent to Minimax
- $N' = 2 * \text{sqrt}(N)$
- Improvement depends on move ordering
- More heuristics needed



## Alpha-Beta

```
int AlphaBeta (Alpha, Beta)
{
    if (Ply == MaxPly) return WhiteToMove ? Eval () : - Eval ();
    GenerateMoves ();
    loop (Move) {
        Make (Move); Ply ++;
        v = - AlphaBeta (~ Beta, - Alpha);
        Ply --; Retract (Move);
        if (v > Alpha) {
            Alpha = v;
            if (Alpha >= Beta) break;
        }
    }
    return Alpha;
}
```

## Alpha Beta at Root

```
Value = AlphaBeta (- Limit, Limit);
```

## Heuristic Improvements

- Move sorting
  - A priori knowledge
  - Evaluation function
  - Captures first
  - Principal variation
  - Killers
  - History
- Staged alpha-beta
  - Iterative depth-first
- Incremental evaluation
- Incremental generation
- Make/retract

## Search Improvements

- Aspiration window for root node
- Scout search, minimal window search
- Hash table
- Quiescence search
- Null moves
- Singular extensions
- Knowledge-based selectivity

## Aspiration Window

```
Value = AlphaBeta (~ Limit, Limit);
if (Value <= ~ Limit) {
    Value = AlphaBeta (~ MAXINT, Limit);
} else if (Value >= Limit) {
    Value = AlphaBeta (~ Limit, MAXINT);
}
```

## Scout

```
int Scout (Alpha, Beta)
{
    if (Ply == MaxPly) return WhiteToMove ? Eval () : - Eval ();
    GenerateMoves ();
    ScoutBeta = Beta;
    loop (Move) {
        Make (Move); Ply ++;
        v = - Scout (- ScoutBeta, - Alpha);
        if (v > Alpha && ScoutBeta != Beta) v = - Scout (- Beta, - Alpha);
        Ply --; Retract (Move);
        if (v > Alpha) {
            Alpha = v; if (Alpha >= Beta) break; ScoutBeta = Alpha + 1;
        }
    }
    return Alpha;
}
```

## Evaluation

- **Material, 1000, 3000, 3000, 5000, 9000**
- **Piece location value tables**
  - Value += Plv [Piece] [To] - Plv [Piece] [From];
- **Second-order evaluation**
  - Mate, stalemate, draw by repetition
  - Centrality, king proximity, mobility, pawn structure
- **Staged evaluation**
  - if (Alpha - T < Value && Value < Beta + T) Evaluate ();

## Shannon's Classification

- **Type A: full width, fixed depth**
- **Type B: fixed width, fixed depth**
  - Width may be function of depth,  $w = f(d)$
- **Type C: variable width, variable depth**
- **Current standard**
  - A plus captures (quiescence)
  - B plus captures

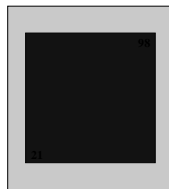
## More Parts

- **Opening library**
  - Databases of 20 000 to 500 000 games
- **Endgame**
  - Special evaluation parameters
  - Rule-based evaluation, KPK
  - Endgame databases, KQKR

## Mailbox Representation

```
#define OFF -1
#define EMPTY 0
#define WP 1
#define WN 2

int Board [120];
```



```
if (Board [From + 11] == EM) {
    Move.From = From; Move.To = From + 11;
}
```

## Bitboard Representation

```
uint64 wp, wn, wb, wr, wq, wk, bp, bn, bb, br, bq, bk, all;
...
ToPattern = KingMoves [FirstOne (wk)] & AllBlack;
Move.From = FirstOne (wk);
Move.To = FirstOne (ToPattern);
...
ToPattern = (wp >> 7) & DiagLeftMask & AllBlack;
```

## Weaknesses

- Limited search depth
- Difficult to perform reliable selectivity
- Strategical evaluation
- Today's chess programs are tactical monsters, but weak in planning and strategy

## Other Methods

- Specific methods (Nim)
  - Colin Vout's car game
  - Mintman
  - The L Game
- Expert systems
  - No success so far...

## Nim

- Three piles of matches
- Take n matches from one of the piles
- The one who takes the last match(es) wins
- Explicit methods to win
- Split numbers into groups of  $2^n$ , the so called Nim sum
- Make an even Nim sum and you are certain to win the game

## Nim

5, 3, 1	4 + 1, 2 + 1, 1	2, 3, 1
0, 3, 1	0, 2 + 1, 1	0, 1, 1
0, 1, 0	0, 1, 0	0, 0, 0

The Nimotron, Condon et al., 1940

## Algorithmic Solutions

- **KPK**
  - Small rule base can play well
- **KRK**
  - Leonardo Torres y Quevedo, 1890

## Inlämningsuppgift I

- Ett program för spelet Kalaha
- Baserat på sökning med standardtekniker
  - Representation?
  - Värdering
  - Alfabeta
  - Iterativ fördjupning
- Diskussion på nästa föreläsning